# A Metadata Calculus for Securing Information Flows

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## Abstract

Traditional approaches to information sharing use a highly conservative approach to deduce the metadata for an output object x derived from input objects  $y_1, y_2, \dots, y_n$  (e.g.: maximum over the security labels of all input objects). Such approaches does not account for functions that explicitly downgrade the value of an object. Consequently, the security labels in traditional approaches tend to monotonically increase as newer objects are derived from existing ones. In this paper we present a novel metadata calculus for securing information flows. The metadata calculus defines a metadata vector space that supports a time varying value function that is computed as a function of the object's metadata and operators + and  $\cdot$  to compute the metadata of an output object that is derived by downgrading, transforming or fusing other objects. We also describe a concrete realization of our metadata calculus wherein the tightness of our value estimates competes in an optimization problem. We present several tradeoffs with space and accuracy and explore a spectrum of solutions ranging from conservative to risk-based value estimates.

### 1 Introduction

Large corporations are slowly being transformed from monolithic, vertically integrated entities, into globally disaggregated value networks, where each member focuses on its core competencies and relies on partners and suppliers to develop and deliver goods and services. The ability of multiple partners to come together, share sensitive business information and coordinate activities to rapidly respond to business opportunities, is becoming a key driver for success.

The defense sector too, has similar, dynamic information sharing needs. Traditional wars between

armies of nation-states are being replaced by highly dynamic missions where teams of soldiers, strategists, logisticians, and support staff, drawn from a coalition of military organizations as well as local (military and civilian) authorities, fight against elusive enemies that easily blend into the civilian population [6]. Securely disseminating mission critical tactical intelligence to the pertinent people in a timely manner will be a critical factor in a mission's success.

While it is clear that information sharing across organizational boundaries is becoming a necessity, it is important for the recipient to ensure that it receives high quality information from the sender. However, for a sender to share high quality information, the sender needs assurance from the recipient that the shared information will not be misused (e.g.: unregulated or unintended information disclosure). Poor quality of information and unauthorized information disclosure can create the risk of legal liability, financial loss, tarnished reputation, or in some environments, a loss of life. Evidently, there is a risk related tradeoff between the quality of information and information misuse. Understanding this tradeoff minimally requires us to quantify the value of information being shared.

Unfortunately, traditional approaches to information sharing suffer from two major drawbacks. First, they use fairly static security labels to tag information, and thus do not attempt to capture dynamic attributes of tactical information such as time sensitivity, accuracy, etc. The value of a piece of information (henceforth, called an object) is computed as a function of its security labels (henceforth, called metadata). For example, Multi-Level Security (MLS) labels such as unclassified, classified, secret, top secret are used to enforce mandatory access control in a military setting; Decentralized Label Management (DLM) labels each object with allow and deny lists and regulates information flows

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	MLS	DLM
Metadata of $x$	$l_x$	$A_x, D_x$
Metadata of $g(x_1, \dots, x_n)$	$max(l_{x_1},\cdots,l_{x_n})$	$\bigcap_{i=1}^n A_{x_i}, \bigcup_{i=1}^n D_{x_i}$

Figure 1: Metadata Calculus

based on these labels.

Second, traditional approaches to information sharing use a highly conservative approach to deduce the metadata for an output object x derived from input objects  $x_1, x_2, \dots, x_n$  (see Figure 1). Such approaches does not account for functions that explicitly downgrade the value of an object. For example, a set of numeric objects may be statistically downgraded using their mean; an image may be downgraded by lowering its resolution, smoothness factor, etc. Consequently, the security labels in traditional approaches tend to monotonically increase as newer objects are derived from existing ones. Ultimately, most of the derived objects receive the highest security label making them inaccessible to most of the users in the organization. As pointed out by the JASON committee report [5], traditional approaches severely constrict the flow of critical information and are thus not appropriate for dynamic settings, where systems and processes evolve rapidly and there are transient needs for sharing tactical, time-sensitive information across organizational bound annot be sure of either the existence, or the proper aries.

In this paper we present a novel metadata calculus for securing information flows. We capture an object's metadata using a vector space  $\mathcal{M}$  and define a metadata calculus that supports the following primitives: (i) a time varying value function  $\Gamma$ based on an object's metadata, and (ii) operators + and  $\cdot$  on the vector space  $\mathcal{M}$  that can be used to compute the metadata for an output object that is derived by downgrading, transforming or fusing other objects. We also describe a concrete realization of our metadata calculus wherein the tightness of our value estimates competes in an optimization problem. We present several tradeoffs with space and accuracy and explore a spectrum of solutions ranging from conservative to risk-based value estimates.

The rest of this paper is organized as follows. Section 2 describes related work on risk based secure information flows. Section 3 describes metadata types and presents an information theoretic

approach to estimating the value of an object. Section 4 describes a calculus for succinctly computing the metadata for an output object that is derived from one or more input objects. Finally we conclude the paper in Section 5.

#### 2 Related Work

There has been significant research on decentralized information labels and assured information sharing within and across multiple organizations [2, 3, 4, 10, 11, 12 in recent years. However, these works primarily focus on the problem of specifying and manipulating the sharing, propagation and downgrading constraints on data. These works also assume appropriate security controls that manipulate, bind and respect these labels are already in place, for example, via a secure distributed runtime language, or some other form of a secure distributed trusted computing base. Clearly, in practice, for the settings described in the introduction, one partner usage of, a secure runtime environment of another partner.

Recently, new approaches based on risk estimation and economic mechanisms have been proposed for enabling the sharing of information in dynamic environments [1, 5]. These approaches are based on the idea that the sender dynamically computes an estimate of the risk of information disclosure in providing information to a receiver based on the secrecy of the information to be divulged and the sender's estimate on the trustworthiness of the recipient. The sender then "charges" the receiver for this estimated risk. The recipient, in turn, can decide which type of information is most useful to him and pay only to access that. Entities would either be given a line of risk credit, or adopt a marketbased mechanism to "purchase risk" using a pseudocurrency. Under the assumption that the line of risk credit or the risk available for purchase in the market is limited, an entity will be encouraged to be frugal with their amassed risk credits and, consequently, reluctant to spend them unnecessarily. Since all information flows are "charged" against expected losses due to unauthorized disclosure and the amount of risk available is limited, an argument is made that the total information disclosure risk incurred by an organization is controlled.

While, as a concept, using risk estimation, charging for risk of information flows, and limited risk credits are promising ideas for enabling information sharing in dynamic environments, the existing work in this area [1, 5] has gaps in how this concept can be realized to enable cross-organizational secure information flows in dynamic environments such as between organizations or partners in a coalition. In [1, 5, 8, 7], while risk is estimated based on the object metadata [9], the actual formulas or examples use static credentials (e.g., the security clearance or category set) of the recipient, rather than a dynamic value of the object. Indeed, the value of most tactical information tends to decrease with time and evolve as the object is downgraded, transformed or fused with other objects. In this paper we present a novel metadata calculus that can be used to succinctly estimate the time varying value of tactical information in a dynamic coalition setting.

# 3 Metadata Model

In this section we describe our metadata model. For the sake of simplicity we include one dynamic attribute, namely time, in our metadata model. We represent the metadata for an object x as a vector  $\vec{x}$  in a vector space  $\mathcal{M}$ .  $\mathcal{M}$  also supports an unary operator that maps  $\vec{x} \in \mathcal{M}$  to value function:  $\Gamma$ :  $\mathcal{M} \rightarrow (\mathcal{F} \rightarrow \mathcal{F})$ , where  $\mathcal{F}$  denotes an integer or real number field. For example,  $\vec{x} = (10, 2)$  and  $\Gamma \vec{x}(t) = \max(10 - 2t, 0)$  or  $\Gamma \vec{x}(t) = 10e^{-2t}$ . The value operator  $\Gamma$  satisfies the following properties:

$$\begin{split} 0 & \leq \Gamma \vec{x}(t) < \infty, \forall t \\ \frac{\partial \Gamma \vec{x}(t)}{\partial t} & \leq 0, \forall t \\ x & \subseteq y \Rightarrow \Gamma \vec{x}(t) \leq \Gamma \vec{y}(t), \forall t \end{split}$$

Constraining the value of object to non-negative integers (or real numbers) may be questionable. One can think of sources of disinformation (misguiding information) to have a negative value. In this paper we do not consider pieces of information that are intended to misguide the recipient. In the absence of disinformation, the value of information is monotonic, that is, if an object x is completely contained in object y, then  $\Gamma \vec{x}(t) \leq \Gamma \vec{y}(t)$ .

The value of an output object x computed as  $g(y_1, y_2, \dots, y_n)$  is computed as shown by an empirical formula in Equation 1, where  $\overline{Y_i} = \{Y_1, \dots, Y_{i-1}, Y_{i+1}, \dots, Y_n\}$  and  $\overline{y_i} = \{y_1, \dots, y_{i-1}, y_{i+1}, \dots, y_n\}$ .

$$\Gamma \vec{x}(t) = \sum_{i=1}^{n} \Gamma \vec{y_i}(t) * \frac{f_{Y_i|X}(y_i|x, B)}{f_{X|\overline{Y_i}}(x|\overline{y_i})}$$
(1)

We use  $f_X$  to denote the probability distribution function for a random variable X. Value computation uses the notion of self-information expressed as  $I(y_i|x) = D(\delta_{y_i} \parallel f_{Y_i|X}(y_i|x)) = -\log(f_{Y_i|X}(y_i|x)),$ where  $D(X \parallel Y)$  denotes KL-divergence between probability distributions X and Y and  $\delta_{u_i}$  denotes the Dirac delta function whose value is one when  $Y_i$  $= y_i$  and zero otherwise. Intuitively self-information  $I(y_i|x)$  denotes the number of additional bits that need to be learnt in order to reconstruct  $y_i$  given that the entity knows the probability distribution  $f_{Y_i|X}$ . Hence,  $2^{-I(y_i|x)} = f_{Y_i|X}(y_i|x)$  denotes the fraction of information about  $y_i$  that may be inferred from x. We remark that exact reconstruction of  $y_i$  may not be required for certain objects (e.g.: geographical location). In such cases, one can replace  $\delta_{y_i}$  by some probability distribution that is centered around  $y_i$ .

We argue that Equation 1 satisfies the intuitive notion of object downgrade, transforms and fusion. In the rest of this section, we demonstrate the applicability of Equation 1 to a wide range of functions  $g(\cdot)$  ranging from arithmetic functions, database operations and cryptographic functions. Figure 2, 3 and 4 show value computations for some sample functions g. We use B to denote background information known to the consumer of object x such as cryptographic secrets.

In the case of bijective arithmetic functions (such as  $x = g(y_1) = y_1 + 1$ ), we note that given x and the function g, one can completely recover all information about  $y_1$ . Hence, the value of x equals the value of  $y_1$  for all time instances t. On the other hand, arithmetic functions such as  $x = y_1^2$  loose information on  $y_1$ ; in particular, given x one can identify two possible values for  $y_1$  (namely,  $\pm \sqrt{x}$ ). In the absence of any background information on  $y_1$ , this results in an entropy loss of one bit; equivalently

g	B	$\Gamma \vec{x}$	note
$x = y_1 + 1$	_	$\Gamma \vec{y_1}(t)$	g is bijective
$x = y_1^2$	_	$\frac{\Gamma \vec{y_1}(t)}{2}$	g is invertible
$x = y_1^2$	$y_1 > 0$	$\Gamma \vec{y_1}(t)$	g is bijective given $B$
$x = \sum_{i=1}^{n} y_i$	$n, \forall i, y_i \sim f_Y$	$0 \le \Gamma \vec{x}(t) \le \sum_{i=1}^n \Gamma \vec{y_i}(t)$	Statistical downgrading

Figure 2: Value Computation for Arithmetic Functions

g	B	$\Gamma \vec{x}$	note
$x = y_1 \bowtie y_2$	_	$2^k * (\Gamma \vec{y_1}(t) + \Gamma \vec{y_2}(t))$	Join operation
$x = y_1 \cup y_2$	_	$\Gamma \vec{y_1}(t) + \Gamma \vec{y_2}(t)$	Union operation
$x = \pi_{y_1} \{ y_1, y_2 \}$	_	$2^{-k} * \Gamma \overrightarrow{\{y_1, y_2\}}$	Project operation
$x = \sigma_p\{y_1, y_2\}$	_	$\frac{ x }{ \{y_1,y_2\} } * \Gamma \overrightarrow{\{y_1,y_2\}}$	Select operation using predicate $p$

Figure 3: Value Computation for Database Functions: Assume, we have two database fields  $Y_1$  and  $Y_2$ . The values  $y_1$  in  $Y_1$  and  $y_2$  in  $Y_2$  are independent and chosen using a uniform distribution between  $(0, 2^k - 1)$ 

g	B	$\Gamma \vec{x}$	note
x = K	_	0	Key $K$ has zero value;
			but knowledge of $K$ affects the value of other objects
$x = E_K(y_1)$	_	0	Ideal encryption
$x = E_K(y_1)$	K	$\Gamma \vec{y_1}(t)$	Ideal encryption
$x = D_{K'}(E_K(y_1))$	$K' \neq K$	0	Ideal decryption
$x = D_K(E_K(y_1))$	K	$\Gamma \vec{y_1}(t)$	Ideal decryption
$x = H_K(y_1)$	K	0	Ideal hash
$x = Sig_K(y_1)$	K	0	Ideal signature

Figure 4: Value Computation for Cryptographic Functions

the value of x is half the value of  $y_1$ . However, the recipient were to know that  $y_1 \geq 0$ , then there is no loss of information. Functions such as sum and average may exhibit different information loss characteristics. For example, let us suppose  $x = y_1 + y_2$ . If the recipient knows that  $0 \leq y_1, y_2 \leq 5$ , then given x = 0 (or 10), it can obtain all information about  $y_1$  and  $y_2$  respectively.

For database operations, we recognize the need to differentiate between union and join operations. Union operates on two sets of the *same type*; for example, let us consider sets of type color  $y_1 = \{red\}$ and  $y_2 = \{\text{blue}\}$ . Consequently, union of two sets does not result in any additional information than the input sets. On the other hand, join operates on two sets of different types; for example, let us consider a set of type  $\langle x\text{-coord}, id \rangle y_1 = \{\langle 10, id_1 \rangle\}$  and a set of type  $\langle y\text{-coord}, id \rangle y_2 = \{\langle 5, id_1 \rangle\}$ . A join on  $y_1$  and  $y_2$  reveals the (x,y) coordinates of the entity  $(id_1)$  and thus has significantly more information than the input sets. To cite another example, let us consider a 128-bit cryptographic key  $K = L \parallel R$ of value V, where L and R denote the left and the right 64-bites of a 128-bit key K. One might argue that the value of L and R is  $2^{-64} * V$ , assuming the key K is randomly chosen over a 128-bit field. Now, let us consider a join of sets of type  $\langle L, kid \rangle$ and  $\langle R, kid \rangle$ , where kid denotes key identifier:  $y_1$  $= \{\langle L_1, kid_1 \rangle\}$  and  $y_2 = \{\langle R_1, kid_1 \rangle\}$ . It is easy to see that the value of x must be significantly higher than the sum of values  $y_1$  and  $y_2$ . Indeed, Equation 1 amplifies the values of  $y_1$  and  $y_2$  by a factor of  $2^{64}$ when deriving the value of x.

For cryptographic operations, we model ideal behavior using a 0/1 value relationship with the input object. For example, using an ideal encryption function  $x = E_K(y_1)$ , the value of x is zero if the recipient does not know K; otherwise, the value of x is equal to the value of  $y_1$ , since the recipient can recover all information about  $y_1$  using the corresponding decryption function D and the key K.

#### 4 Metadata Calculus

In this section, we describe a metadata calculus using two binary operators on the metadata vector space  $\mathcal{M}$ : vector addition +:  $\mathcal{M} \times \mathcal{M} \to \mathcal{M}$  and scalar multiplication :  $\mathcal{F} \times \mathcal{M} \to \mathcal{M}$ , where  $\mathcal{F}$  denotes a field such as integers or real numbers. These

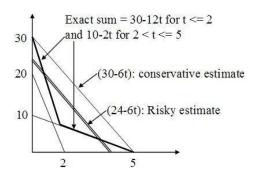


Figure 5: Conservative Vs Risky '+' Operator

binary operators satisfy the following homomorphic properties:

- $\vec{x} = \vec{y_1} + \vec{y_2} \Leftrightarrow \Gamma \vec{x}(t) = \Gamma \vec{y_1}(t) + \Gamma \vec{y_2}(t)$  for all t.
- $\vec{x} = a \cdot \vec{y_1} \Leftrightarrow \Gamma \vec{x}(t) = a * \Gamma \vec{y_1}(t)$  for all t.

In addition, they also satisfy the following intuitive properties:

- Commutative: For any  $\vec{y_1}$ ,  $\vec{y_2} \in \mathcal{M}$ ,  $\vec{y_1} + \vec{y_2} = \vec{y_2} + \vec{y_1}$ .
- Associative: For any  $\vec{y_1}$ ,  $\vec{y_2}$ ,  $\vec{y_3} \in \mathcal{M}$ ,  $\vec{y_1} + (\vec{y_2} + \vec{y_3}) = (\vec{y_1} + \vec{y_2}) + \vec{y_3}$ .
- Zero vector  $\vec{0}$ : For any  $\vec{y_1} \in \mathcal{M}$ ,  $\vec{y_1} + \vec{0} = \vec{y_1}$ .
- Distributive over + in  $\mathcal{M}$ : For any  $a \in \mathcal{F}$ ,  $\vec{y_1}, \vec{y_2} \in \mathcal{M}, a \cdot (\vec{y_1} + \vec{y_2}) = a \cdot \vec{y_1} + a \cdot \vec{y_2}$ .
- Distributive over + in  $\mathcal{F}$ : For any  $a, b \in \mathcal{F}$ ,  $\vec{y_1} \in \mathcal{M}$ ,  $(a+b) \cdot \vec{y_1} = a \cdot \vec{y_1} + b \cdot \vec{y_1}$ .
- Distributive over  $\cdot$  in  $\mathcal{M}$ : For any  $a, b \in \mathcal{F}$ ,  $\vec{y_1} \in \mathcal{M}$ ,  $a \cdot (b \cdot \vec{y_1}) = (ab) \cdot \vec{y_1}$ .
- Scalar 1 in  $\mathcal{F}$ : For any  $\vec{y_1} \in \mathcal{M}$ ,  $1 \cdot \vec{y_1} = \vec{y_1}$ .

Based on the properties described above, it is easy to see that when x is computed as  $g(y_1, y_2, \dots, y_n)$  then the metadata  $\vec{x}$  can be computed as shown in Equation 2. Indeed give the homomorphic properties on the  $\mathcal{M}$ , we can show that Equation 2 implies Equation 1 for all time t.

$$\vec{x} = \sum_{i=1}^{n} \frac{f_{Y_i|X}(y_i|x, B)}{f_{X|\overline{Y_i}}(x|\overline{y_i})} \cdot \vec{y_i}$$
 (2)

#### 4.1 Realizing the Metadata Calculus

In this section, we describe a concrete instantiation of metadata calculus. Unfortunately, there exists no vector space that satisfies all the required homomorphic properties. In this section, we describe a metadata vector space and value functions that satisfy a weaker notion of homomorphism as shown in Equation 3. It follows from Equation 3 that our metadata calculus makes conservative estimates on object values.

$$\vec{x} = a \cdot \vec{y_1} \Leftrightarrow \Gamma \vec{x}(t) = a * \Gamma \vec{y_1}(t), \forall t$$
  
$$\vec{x} = \vec{y_1} + \vec{y_2} \Rightarrow \Gamma \vec{x}(t) \ge \Gamma \vec{y_1}(t) + \Gamma \vec{y_2}(t), \forall t$$
 (3)

We use a metadata space  $\mathcal{M} = \mathcal{Z} \times \mathcal{Z}$ , where  $\mathcal{Z}$  denotes integer field. Given  $\vec{x} = (c_0, c_1)$ ,  $\Gamma \vec{x}(t) = \max(c_0 - c_1 * t, 0)$ . Given  $\vec{x_1} = (c_0^1, c_1^1)$  and  $\vec{x_2} = (c_0^2, c_1^2)$ , the + and  $\cdot$  operators are defined as follows:

$$a \cdot \vec{x_1} = (a * c_0^1, a * c_1^1)$$

$$\vec{x_1} + \vec{x_2} = \left(c_0^1 + c_0^2, \frac{c_0^1 + c_0^2}{\max\left(\frac{c_0^1}{c_1^1}, \frac{c_0^2}{c_1^2}\right)}\right)$$

Figure 5 illustrates the + operator on  $\vec{y_1} = (10, 2)$  and  $\vec{y_2} = (20, 10)$ . It is easy to see that  $\Gamma \vec{y_1}(t) + \Gamma \vec{y_2}(t)$  is:

$$\Gamma \vec{y_1}(t) + \Gamma \vec{y_2}(t) = \begin{cases} 30 - 12t & \text{if } t \le 2\\ 10 - 2t & \text{if } 2 < t \le 5 \end{cases}$$

It is easy to that the above equation cannot be represented by a straight line and thus cannot be mapped into a metadata vector in  $\mathcal{M}$ . Hence, we choose the least conservative straight line (30-6t) such that  $\Gamma \vec{y_1}(t) + \Gamma \vec{y_2}(t) \leq 30-6t$  for all t. Indeed, there are several options to ensure that our value estimates are tighter all of which can be modeled as optimization problems.

• First, we can increase the dimensionality of the metadata vector space and use a high order polynomial for  $\Gamma \vec{x}(t)$ . It is easy to see that proposed metadata calculus can be extended to all value functions that are polynomial in time t. We note that increasing the dimensionality of the metadata vector allows us to compute tighter value estimates at the cost of higher storage cost.

- Second, we can represent  $\vec{x}$  as k tuples where each tuple describes a straight line within some time interval. We note that when x is computed as a function of  $y_1, \dots, y_n$ , then the value of x may be represented by at most n linear constraints. For any given constant  $k \leq n$ , we can compute a set of k linear constraints that tightly bounds the set of n linear constraints. We note that increasing k allows us to compute tighter value estimates at the cost of higher storage cost.
- Third, we could permit bounded violations to the constraint  $\Gamma(\overrightarrow{y_1} + \overrightarrow{y_2})(t) \geq \Gamma \overrightarrow{y_1}(t) + \Gamma \overrightarrow{y_2}(t)$ for some instants t. One can quantify the risk  $(r^{+})$  in a value estimate using the area enclosed by the region wherein our value estimate is lower than the true value of the object; similarly, one can quantify overestimation  $(r^{-})$  using the area enclosed by the region wherein our value estimate is higher than the true value of the object. We formulate two optimization problems that allow us to trade off the conservativeness and tightness in our estimates. First, we can restrict the risk in our value estimate to at most X% of the value of the object (averaged over its lifetime). Second, we can attempt to minimize a function of risk and overestimation, say  $\alpha * r^+ - r^-$ , for some  $\alpha > 0$ .

#### 5 Conclusion

In this paper we have presented a novel metadata calculus for securing information flows in a tactical setting. The metadata calculus defines a metadata vector space that supports a time varying value function that is computed as a function of the object's metadata and operators + and  $\cdot$  to compute the metadata of an output object that is derived by downgrading, transforming or fusing other objects. We have also described a concrete realization of our metadata calculus using a value function that is polynomial in time t. We have formulated the problem of finding tight value estimates as various optimization problems. These formulations model various tradeoffs with space and accuracy and explore a spectrum of solutions ranging from conservative to risk-based value estimates.

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